

Note: All questions are compulsory.

Question 1 (8 Marks)

Let the P₁, P₂ and P₃ be the three products to be manufactured. Then the data are as follows:

Products	Product ingredients			Inert Ingredients
	A	B	C	
P ₁	5 %	10%	5%	80%
P ₂	5%	5%	10%	80%
P ₃	20%	5%	10%	65%
Cost per kg (₹)	64	16	40	16

Cost of Product P₁

$$= 5\% \times ₹64 + 10\% \times ₹16 + 5\% \times ₹40 + 80\% \times ₹16 = ₹19.60 \text{ per kg}$$

Cost of Product P₂

$$= 5\% \times ₹64 + 5\% \times ₹16 + 10\% \times ₹40 + 80\% \times ₹16$$

$$= ₹20.80 \text{ per kg.}$$

Cost of Product P₃

$$= 20\% \times ₹64 + 5\% \times ₹16 + 10\% \times ₹40 + 65\% \times ₹16$$

$$= ₹28.00 \text{ per kg.}$$

Let x₁, x₂, and x₃ be the quantity (in kg) of P₁, P₂, and P₃ respectively to be manufactured. The LP problem can be formulated:

Objective function: (2 marks)

$$\text{Maximize } Z = (\text{Selling Price} - \text{Cost Price}) \times \text{Quantity of Product}$$

$$= (₹32.60 - ₹19.60) x_1 + (₹34.80 - ₹20.80) x_2 + (₹36.00 - ₹28) x_3$$

$$= 13x_1 + 14x_2 + 8x_3$$

Subject to Constraints: (6 marks)

$$\frac{1}{20}x_1 + \frac{1}{20}x_2 + \frac{1}{5}x_3 \leq 100$$

Or $x_1 + x_2 + 4x_3 \leq 2,000$

$$\frac{1}{10}x_1 + \frac{1}{20}x_2 + \frac{1}{20}x_3 \leq 180$$

Or $2x_1 + x_2 + x_3 \leq 3,600$

$$\frac{1}{20}x_1 + \frac{1}{10}x_2 + \frac{1}{10}x_3 \leq 120$$

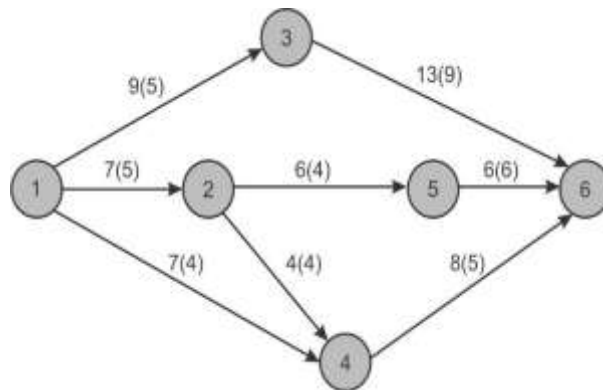
Or $x_1 + 2x_2 + 2x_3 \leq 2,400$

$$x_1 \leq 30$$

and $x_1, x_2, x_3 \geq 0$

Question 2 (8 Marks)

The **Network** for the given problem (2 marks)



Different Paths, Normal Duration and Minimum Duration:

Path	Normal Duration (Days)	Minimum Duration (Days)
1-3-6	22 (9 + 13)	14 (5 + 9)
1-2-5-6	19 (7 + 6 + 6)	15 (5 + 4 + 6)
1-2-4-6	19 (7 + 4 + 8)	14 (5 + 4 + 5)
1-4-6	15 (7 + 8)	9 (4 + 5)

Critical Path is 1-3-6

Total Cost of the Project for the Normal Duration: (1 mark)

$$\begin{aligned}
 &= \text{Normal Cost} + \text{Overhead Cost} + \text{Penalty Cost} = \text{₹}6,000 + \text{₹}150 \times 22 \text{ Days} \\
 &+ \text{₹}80 \times 3 \text{ Days} \\
 &= \text{₹}9,540
 \end{aligned}$$

Crashing First Step: (2 mark)

Let us now crash activities on the Critical Path.

Activity	ΔT	$\Delta C/\Delta T$	Remark
1-3	4	100	Least Cost Slope
3-6	4	210	

As activity 1-3 has least cost slope, **crash activity 1-3 by 3 days at a crash cost of ₹100 per day.**

Total Cost of the Project for the 19 Days:

$$\begin{aligned}
 &= \text{Normal Cost} + \text{Overhead Cost} + \text{Crashing Cost} \\
 &= \text{₹}6,000 + \text{₹}150 \times 19 \text{ Days} + \text{₹}100 \times 3 \\
 &\quad \text{Days} \\
 &= \text{₹}9,150
 \end{aligned}$$

The Various Paths in the Network with Revised Duration are:

$$1-3-6 \text{ with Project Duration} = 19 \text{ Days (Critical Path.1)}$$

1-2-5-6 with Project Duration = 19 Days (Critical Path.2)

1-2-4-6 with Project Duration = 19 Days (Critical Path.3)

1-4-6 with Project Duration = 15 Days

Crashing Second Step: (2 marks)

Let us now crash activities on the Critical Paths.

Critical Path	Activity	ΔT	$\Delta C/\Delta T$	Remark
1	1-3	1	100	Least Cost Slope
	3-6	4	210	
2	1-2	2	90	
	2-5	2	50	Least Cost Slope
	5-6	-	-	-
3	1-2	2	90	
	2-4	-	-	-
	4-6	3	60	Least Cost Slope

Possible Crashing Alternatives are:

(1 mark)

Critical Path- Activities	1-3, 2-5 & 4-6	1-3 & 1-2*
Cost Slopes ($\Delta C/\Delta T$)	₹210 (₹100 + ₹50 + ₹60)	₹190 (₹100 + ₹90)
Remark	Independent Activities	Independent Activity + Common Activity*

As crashing cost per day for every alternative is greater than ₹150 i.e. Overhead Cost per day. Therefore, any reduction in the duration of project will increase the cost of project completion.

Hence, the **Lowest Cost of Completion** is ₹9,150 with the **Completion Time** of 19 Days.

Question 3 (10 Marks)

(a) **Workings**

Statement Showing “Cost Driver Rate” (3 Marks)

Overhead	Cost(₹) - Lacs	Cost Driver	Cost Driver Rate (₹)
Production Line Cost	2,310	60,000 Machine Hrs.	3,850 per hr. <u>2,310lacs</u> 60,000hrs.
Transportation Cost			
Delivery Related (60%)	540	640 Deliveries	84,375 per delivery <u>540lacs</u> 640delivery
Distance Related (40%)	360	2,25,000 Kms.	160 per km <u>360lacs</u> 2,25,000kms.

(i) Forecast Total Cost using Activity Based Costing Principles (4 Marks)

Elements of Cost		
Material		4,75,000.00
Labour		2,50,000.00
Overhead		
Production Line Cost ($3,850 \times 6$ hrs.)		23,100.00
Transportation Cost -		
Delivery Related	$\frac{84,375}{10 \text{ cars}}$	8,437.50
Distance Related	$\frac{160 \times 50,000 \text{ kms}}{1,000 \text{ cars}}$	8,000.00
Total		7,64,537.50

(ii) Calculation of Cost Gap Between Forecast Total Cost and the Target Total Cost (3 Marks)

Particulars	Amount (₹)
Target Selling Price	9,75,000.00
Less: Operating Profit Margin (25%)	2,43,750.00
Target Cost (Target Selling Price – Operating Profit)	7,31,250.00
Forecast Total Cost	7,64,537.50
Cost Gap ($7,64,537.50 - 7,31,250$)	33,287.50

Question 4 (8 Marks)

First of all, random numbers 00 – 99 are allocated in proportion to the probabilities associated with demand as given below: (1 Mark)

Demand	Probability	Cumulative Probability	Random Nos.
0	0.05	0.05	00 – 04
1	0.10	0.15	05 – 14
2	0.30	0.45	15 – 44
3	0.45	0.90	45 – 89
4	0.10	1.00	90 – 99

Based on the ten random numbers given, we simulate the demand per day in the table given below: It is given that stock in hand is 8 units and stock on order is 6 units (expected to receive on next day).

Let us now consider both the options stated in the Problem.

Option-A (3 Marks)

Order 5 books when the inventory at the beginning of the day plus orders outstanding is less than 8 books:

Day	Random No.	Sales Demand	Op. Stock (in hand)	Qty. Order	Qty. Recd. at End of the Day	Total Qty. on Order	Closing Stock
1	89	3	8	---	---	6	5
2	34	2	5	---	6	---	9
3	78	3	9	---	---	---	6
4	63	3	6	5	---	5	3
5	61	3	3	---	---	5	0

6	81	3	0	5	5	5	2
7	39	2	2	5	---	10	0
8	16	2	0	---	5	5	3
9	13	1	3	---	5	---	7
10	73	3	7	5	---	5	4

Carrying Cost = `195 (39 Books × `5)

Ordering Cost = `400 (4 Orders × `100)

Total Cost = `595 (`195 + `400)

Option-B(3 Marks)

Order 8 Books, when the inventory at the beginning of the day plus orders outstanding is less than 8 books:

Day	Random No.	Sales Demand	Op. Stock (in hand)	Qty. Order	Qty. Recd. at End of the Day	Total Qty. on Order	Closing Stock
1	89	3	8	---	---	6	5
2	34	2	5	---	6	---	9
3	78	3	9	---	---	---	6
4	63	3	6	8	---	8	3
5	61	3	3	---	---	8	0
6	81	3	0	---	8	---	5
7	39	2	5	8	---	8	3
8	16	2	3	---	---	8	1
9	13	1	1	---	8	---	8
10	73	3	8	---	---	---	5

Carrying Cost = `225 (45 Books × `5)

Ordering Cost = `200 (2 Orders × `100)

Total Cost = `425 (`225 + `200)

Recommendation

Since **Option B** has *lower cost*, Manager should order 8 books. (1 Mark)

Question 5 (8 Marks)

Preparation of Production Cost Budget for 50,000 units for the year 2014 (4 Marks)

Particulars	Cost Per Unit	TotalAmount (`)
Materials (W.N.-1)	1.645	82,237.50
Wages (W.N.-2)	1.43	71,500.00
Variable Overhead	0.50	25,000.00
Fixed Overhead (`35,000 × 110%)	0.77	38,500.00
Total Cost	4.345 (Approx.)	2,17,237.50

Working Notes

1. Material Cost- (2 Marks)

(a) Increase in Material Price in the Year 2013-

$$= \frac{\text{Actual Cost per unit in 2013} - \text{Budgeted Cost per unit in 2013}}{\text{Budgeted Cost per unit in 2013}} \times 100$$

$$= \frac{\frac{`53,750}{43,000 \text{ units}} - `1}{`1} \times 100$$

$$= 25\%$$

(b) Material Required to Produce 50,000 units-

$$= \frac{42,000 \text{ units}}{39,900 \text{ units}} \times 50,000 \text{ units}$$

$$= 52,632 \text{ units (rounded)}$$

(c) Increased Cost for 50,000 units in the Year 2014-

$$= \frac{\text{` } 53,750}{43,000 \text{ units}} \times 125\% \times 52,632$$

$$\text{` } 82,237.50$$

Wages- (2 Marks)

Rate *per hour* in 2014-

$$\frac{\text{Wages Paid in the Year 2013}}{\text{Actual Units Produced}} + \text{` } 0.20$$

$$= \frac{\text{` } 44,660}{40,600 \text{ units}} + \text{` } 0.20$$

$$= \text{` } 1.30$$

(b) Wages to be paid for 50,000 units i.e. for 50,000 hours (1 hour per unit). When the labour efficiency is 90% only, then Total Wages will be-

$$= 50,000 \text{ hours} \times \frac{110}{100} \times \text{` } 1.30$$

$$= \text{` } 71,500$$

Note: Fixed Overhead can also be calculated on the basis of previous year's budgeted figure.

Variable Overhead may also be calculated by taking ` 1 per unit.

This question can also be solve by taking 50,000 hrs. as 90% of total hrs. required to produce the 50,000 units.

Question 6 (8 Marks)

(i) **Standard Price per Kg. of Direct Material (2 marks)**

$$\begin{aligned} \text{Material Price Variance} &= \text{Standard Cost of Actual Quantity} - \text{Actual Cost} \\ \Rightarrow 5,000 \text{ (F)} &= \text{Standard Cost of Actual Quantity} - \text{` } 5,20,000 \\ \text{Standard Cost of Actual Quantity} &= \text{` } 5,20,000 + \text{` } 5,000 \\ &= \text{` } 5,25,000 \end{aligned}$$

$$\begin{aligned} \text{Standard Cost of Actual Quantity} &= \text{Standard Price per Kg.} \times \text{Actual Quantity} \\ \text{` } 5,25,000 &= \text{Standard Price per Kg.} \times 1,05,000 \text{ Kg.} \end{aligned}$$

$$\begin{aligned} \text{Standard Price per Kg.} &= \frac{\text{` } 5,25,000}{1,05,000 \text{ Kg.}} \\ &= \text{` } 5 \end{aligned}$$

(ii) **Standard Quantity for each unit of output (1 ½ marks)**

$$\begin{aligned} \text{Material Usage Variance} &= \text{Standard Cost of Standard Quantity for Actual} \\ &\quad \text{Output} - \text{Standard Cost of Actual Quantity} \\ 25,000 \text{ (A)} &= \text{Standard Cost of Standard Quantity for Actual} \\ &\quad \text{Output} - ` 5,25,000 \end{aligned}$$

$$\begin{aligned} \text{Standard Cost of Standard Quantity for Actual Output} \\ &= ` 5,25,000 - ` 25,000 \\ &= ` 5,00,000 \end{aligned}$$

$$\begin{aligned} \text{Standard Cost of Standard Quantity for Actual Output} \\ &= \text{Standard Price per Kg.} \times \text{Standard Quantity for} \\ &\quad \text{Actual Output} \\ \Rightarrow ` 5,00,000 &= ` 5 \times \text{Standard Quantity for Actual Output} \end{aligned}$$

$$\begin{aligned} \text{Standard Quantity for Actual Output} \\ &= \frac{` 5,00,000}{` 5} \\ &= 1,00,000 \text{ Kg.} \end{aligned}$$

$$\begin{aligned} \text{Standard Quantity for each unit of output} \\ &= \frac{1,00,000 \text{ Kg.}}{10,000 \text{ units}} \\ &= 10 \text{ Kg.} \end{aligned}$$

(i) Standard Rate of Direct Labour Hour (1 ½ marks)

$$\begin{aligned} \text{Direct Labour Rate Variance} &= \text{Standard Cost of Actual Time} - \text{Actual Cost} \\ 15,500 \text{ (A)} &= \text{Standard Cost of Actual Time} - ` 3,08,000 \\ \text{Standard Cost of Actual Time} &= ` 3,08,000 - ` 15,500. \\ &= ` 2,92,500 \end{aligned}$$

$$\begin{aligned} \text{Standard Cost of Actual Time} &= \text{Standard Rate per hr.} \times \text{Actual Hours} \\ ` 2,92,500 &= \text{Standard Rate per hr.} \times 19,500 \text{ hrs.} \end{aligned}$$

$$\text{Standard Rate per hr.} = ` 2,92,500 / 19,500 \text{ hrs.} = 15$$

(i) Standard Time for Actual Production (1 ½ marks)

$$\begin{aligned} \text{Labour Efficiency Variance} &= \text{Standard Cost of Standard Time for Actual Production} - \text{Standard Cost of Actual Time} \\ 7,500 \text{ (F)} &= \text{Standard Cost of Standard Time for Actual Production} - ` 2,92,500 \\ \text{Standard Cost of Standard Time for Actual Production} &= ` 2,92,500 + ` 7,500 = ` 3,00,000 \end{aligned}$$

$$\begin{aligned} \text{Standard Cost of Standard Time for Actual Production} &= \text{Standard Rate per hr.} \times \text{Standard Time for Actual Production} \\ 300000 &= ` 15 \times \text{Standard Time for Actual Production} \\ \text{Standard Time for Actual Production} &= 300000/15 = 20000 \text{ hours} \end{aligned}$$

(ii) Standard Variable Overhead Rate (1 1/2 marks)

$$\begin{aligned} \text{Variable Overhead Variance} &= \text{Standard Variable Overheads for Production} \\ &\quad - \text{Actual Variable Overheads} \\ 10,000 \text{ (A)} &= \text{Standard Variable Overheads for Production} \\ &\quad - ` 4,10,000 \\ \text{Standard Variable Overheads for Production} &= ` 4,10,000 - ` 10,000 = ` 4,00,000 \end{aligned}$$

$$\begin{aligned} \text{Standard Variable Overheads for Production} &= \text{Standard Variable Overhead Rate Unit} \times \text{Actual Production (Units)} \\ ` 4,00,000 &= \text{Standard Variable Overhead Rate Unit} \times 10000 \text{ units} \end{aligned}$$

Standard Variable Overhead Rate Unit = 40

Or

Standard Variable Overheads for Production = Standard Variable Overhead Rate per Hr × Std Hrs for Actual Production

4,00,000 = Standard Variable Overhead Rate per Hour × 20,000 hrs

Standard Variable Overhead Rate *per hour* = 20
